

Modeling Soil Test Phosphorus and Potassium Calibration Data

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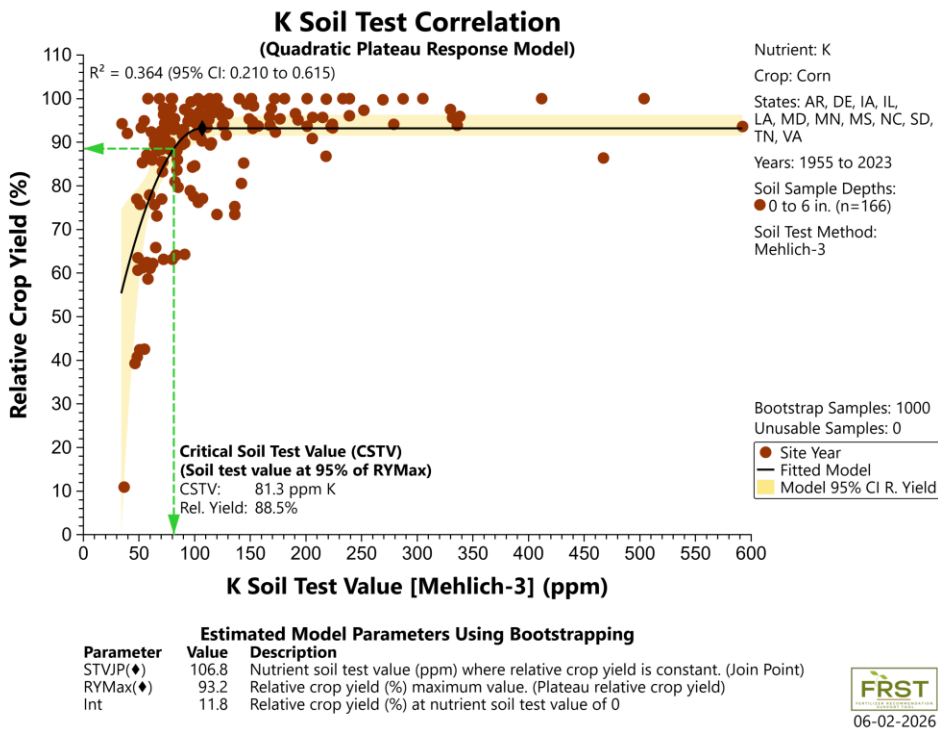
SERA-6, MASTPAWG, and NRSP11

June 2026

Phosphorus and potassium fertilizer recommendations are based on:

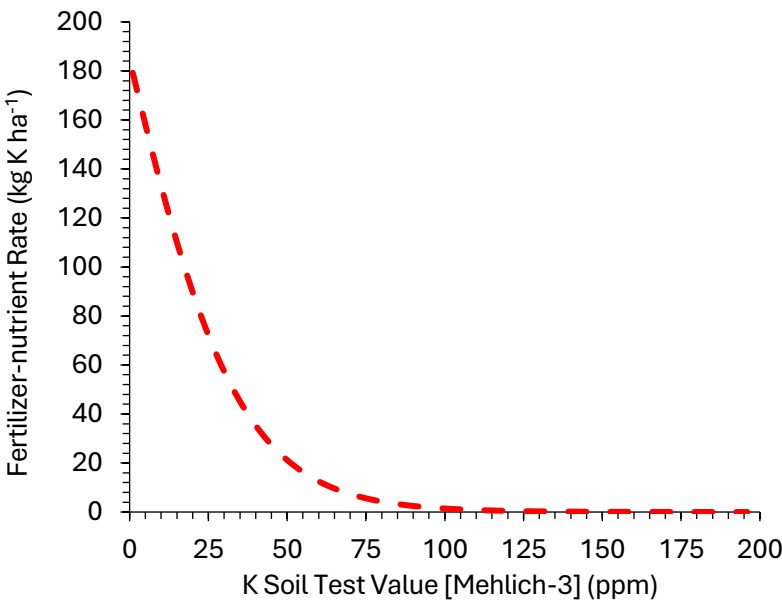
Soil test correlation

Identify the critical soil test value (CSTV)



Soil test calibration

Estimate the fertilizer-nutrient rate required to achieve optimal yield across soil test values (STVs)



Why test soil test calibration frameworks?

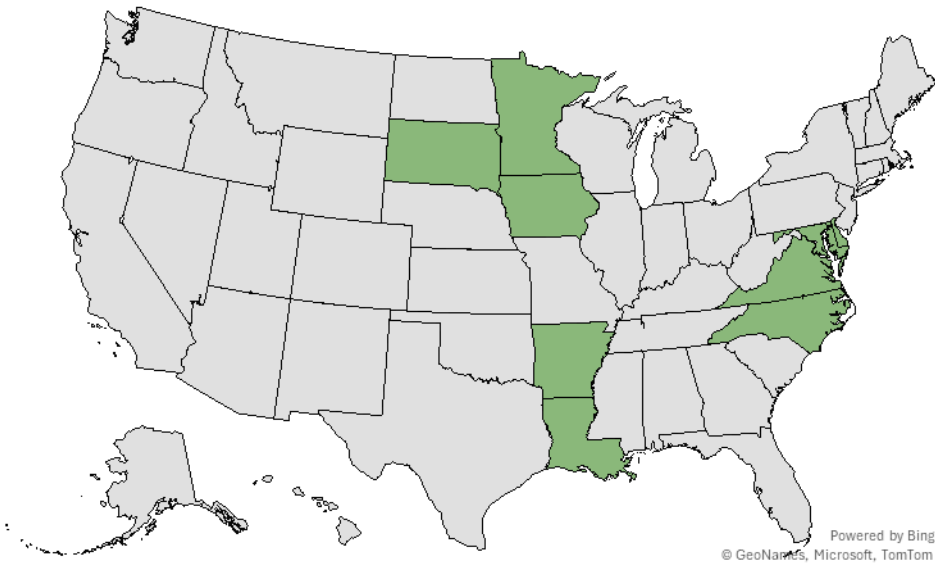
- **Relatively few soil test calibration frameworks for estimating fertilizer-nutrient requirements have been published**
- **The strengths and limitations of calibration frameworks have rarely been evaluated**
- **Calibration frameworks present some methodological challenges:**
 - Multicollinearity among predictor variables in regression-based approaches
 - Discontinuous recommendation functions in class-based methods
 - Limited flexibility for incorporating uncertainty and risk preferences
- **The lack of a standardized calibration framework creates challenges for improving soil test-based fertilizer recommendations**

Objectives

- (i) Evaluate how soil test calibration frameworks influence estimated fertilizer-P and -K rate recommendations**
- (ii) Identify a calibration framework suitable for implementation in the FRST decision-support tool**

Dataset selection for modeling fertilizer-nutrient rate

Representation across geographic regions (nine U.S. states), crops (corn and soybean), nutrients (P and K), and soil test extractants (Mehlich-1 and -3, Olsen, and Bray-1)



Dataset	# site-years	STV range	CSTV
		(mg kg ⁻¹)	
1 Mehlich-3 K soybean	45	46–353	94
2 Mehlich-1 K soybean	41	16–196	46
3 Olsen P corn	35	3–31	5.0
4 Bray-1 P corn	25	2–59	11
5 Mehlich-3 K corn	134	37–592	70

Fertilizer-P and -K application rates ranged from 0 to 75 kg P ha⁻¹ and 0 to 224 kg K ha⁻¹

Source: Bourns et al., 2025; Lyons et al., 2021; Mallarino & Blackmer, 1992; Mallarino et al., 2009; Parvej et al., 2018; Popp et al., 2020; Williams et al., 2018

Dataset preparation

Input trial data

Trial's mean STK (mg kg ⁻¹)	Fertilizer-K application rates (kg K ha ⁻¹)	Absolute crop yield (kg ha ⁻¹)	RY (%)
72	0	2892	77
	40	3195	86
	80	3652	98
	120	3685	99
	160	3733	100

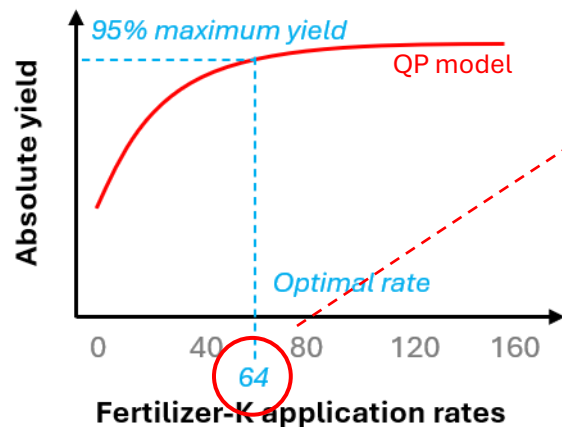
Two-step calibration framework

Trial's mean STK (mg kg ⁻¹)	Optimal fertilizer-K rate (kg K ha ⁻¹)
72	64

Single-step calibration framework

Trial's mean STK (mg kg ⁻¹)	Fertilizer-K application rates (kg K ha ⁻¹)	RY (%)
72	0	77
	40	86
	80	98
	120	99
	160	100

Determine the optimal fertilizer-nutrient rate



Modeling approaches for fertilizer-nutrient rate estimation

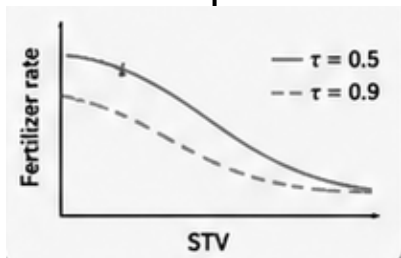
Two-step calibration framework

Quantile regression

Declining sigmoidal
quantile regression

Process

- Fit declining sigmoidal model
- Estimate fertilizer-nutrient requirement at $\tau = 0.5$ (median)
 $\tau = 0.9$ (upper-bound)



Output

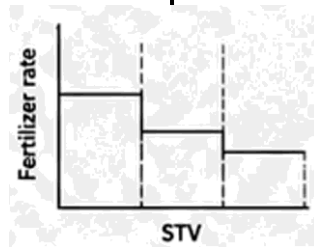
Continuous fertilizer
recommendation curve

STCI

Soil test class-interval

Process

- Define STV class intervals
- Calculate the median fertilizer-nutrient rate in each interval



Output

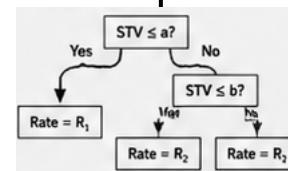
Stepwise fertilizer
recommendation by class
interval

CART

Classification and
Regression Tree

Process

- Build a regression tree using recursive partitioning
- Identify STV thresholds that best explain fertilizer-nutrient rate variation
- Calculate the median fertilizer-nutrient rate within each STV threshold



Output

Stepwise fertilizer
recommendation by STV
threshold

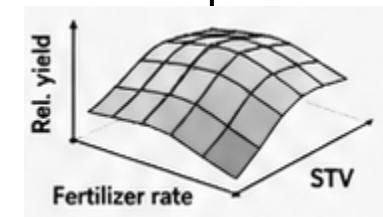
Single-step calibration framework

ENET

Elastic Net Regression

Process

- Model relative yield as a function of STV and fertilizer-nutrient application rates
- Predict fertilizer-nutrient rate for target relative yield (e.g., 95%)



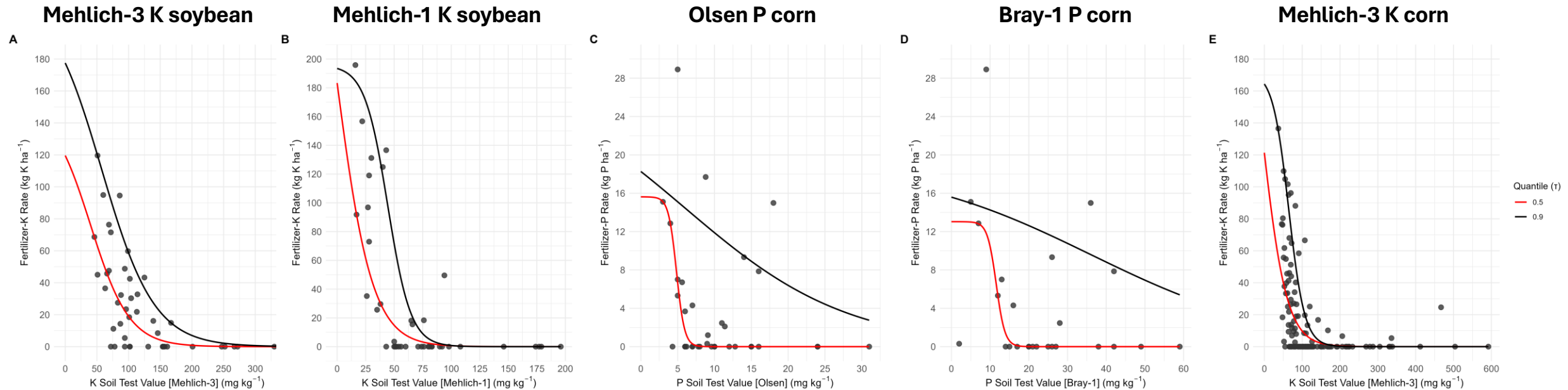
Output

Predicted fertilizer
recommendation surface

Results

Overall, all frameworks predicted declining fertilizer-nutrient requirements with increasing STV; however, the magnitude and pattern of decline varied among approaches and datasets

Quantile regression (nonlinear declining sigmoidal quantile regression)



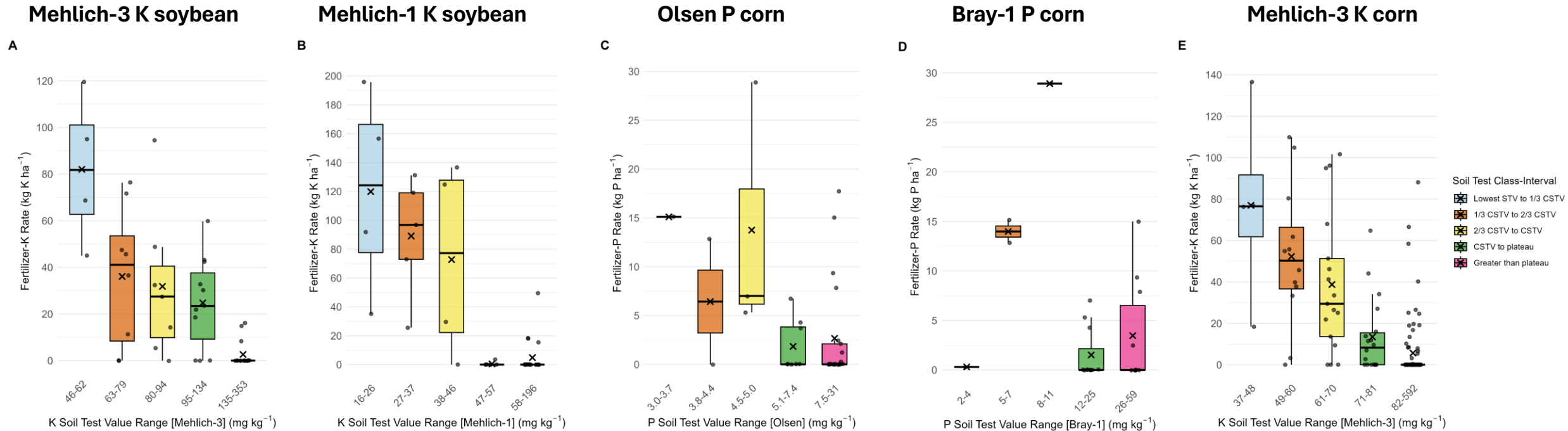
Advantages

- The 0.5 and 0.9 quantiles represent the median and upper bound of the fertilizer-nutrient requirement
- Provides a continuous function to estimate fertilizer-nutrient rate across STVs
- Provides a range of fertilizer-nutrient rates at the same STV

Limitations

- The model's performance depends on the dataset structure
- Data processing to determine the optimal fertilizer-nutrient rate

STCI (Soil Test Class-Interval)



Advantages

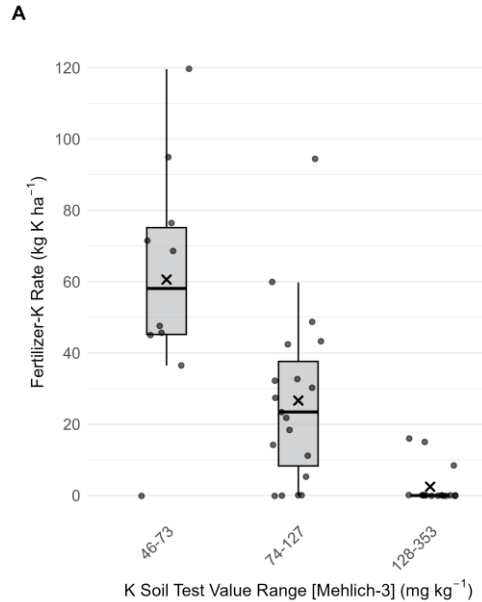
- Transparent and assumption-free summary of data
- Computationally simple and easy to communicate with end users
- Can reduce the influence of scatter observations (e.g., Olsen P corn)

Limitations

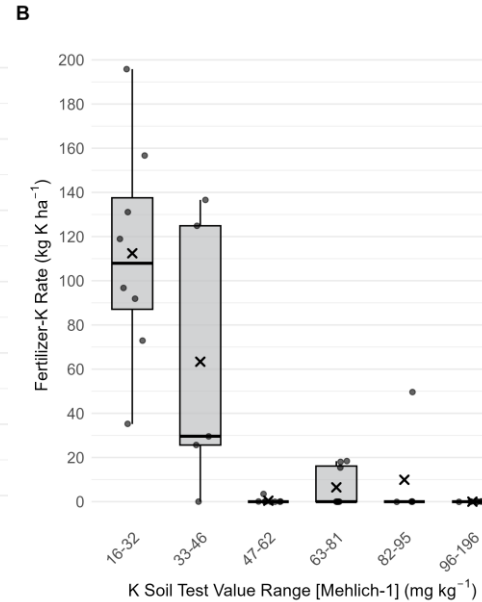
- Requires predefined soil test class boundaries
- Stepwise behavior (sensitive to the number and distribution of the observations)
- Data processing to determine the optimal fertilizer-nutrient rate

CART (Classification and Regression Tree)

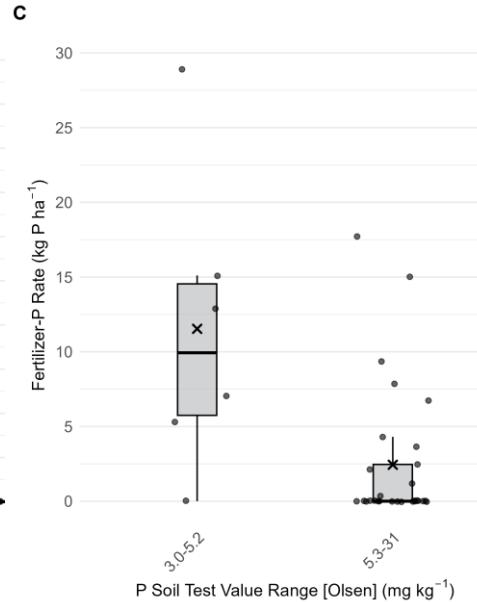
Mehlich-3 K soybean



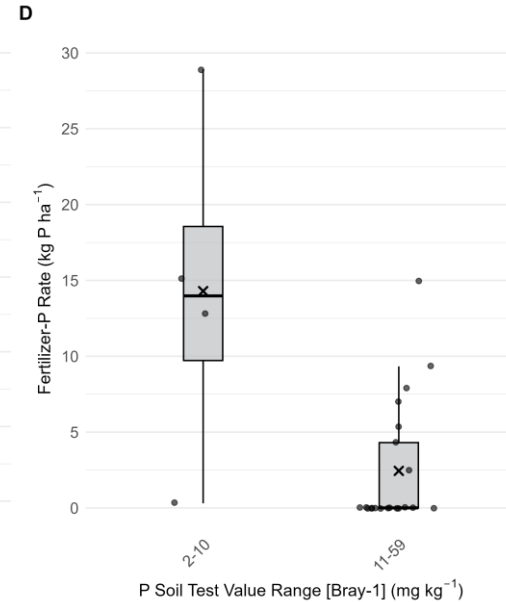
Mehlich-1 K soybean



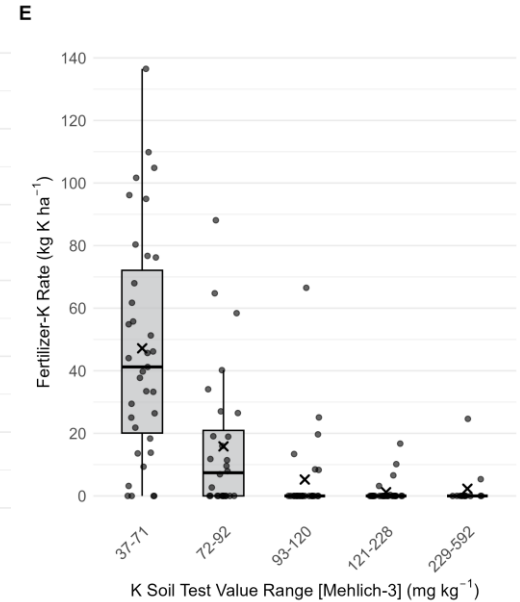
Olsen P corn



Bray-1 P corn



Mehlich-3 K corn



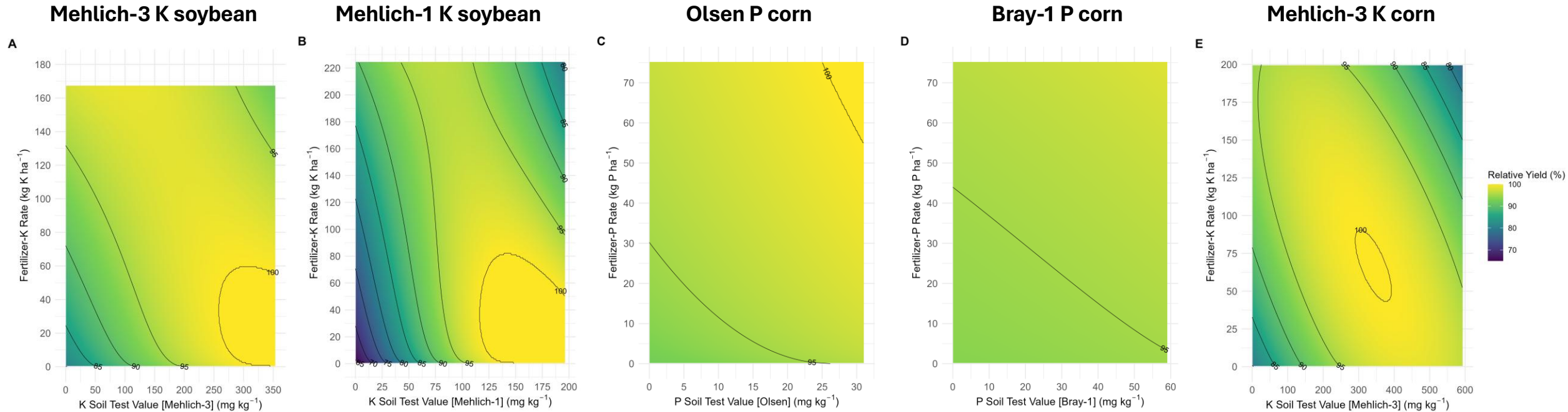
Advantages

- Effective at capturing changes in fertilizer-nutrient requirements
- Easy to communicate with end users

Limitations

- Stepwise behavior may oversimplify nutrient response patterns
- Data processing to determine the optimal fertilizer-nutrient rate

ENET (Elastic Net Regression)



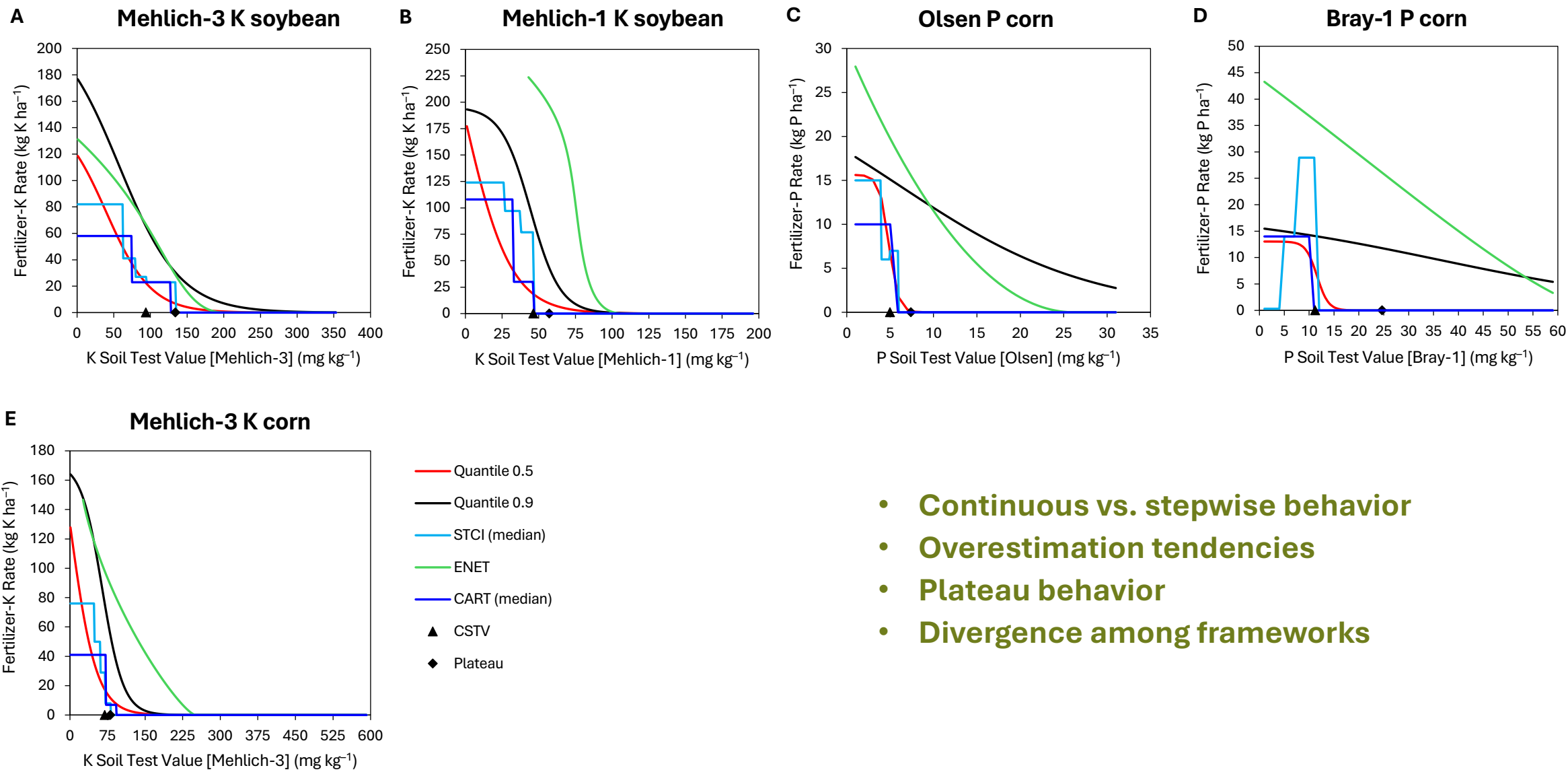
Advantages

- Use of the full experimental dataset without requiring prior estimation of an optimal fertilizer-nutrient rate

Limitations

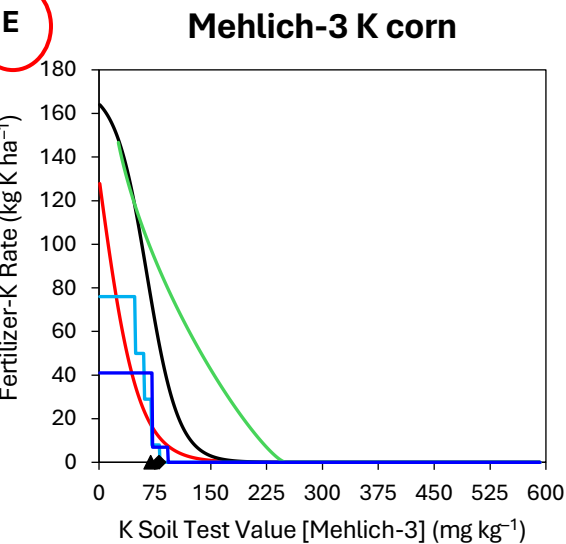
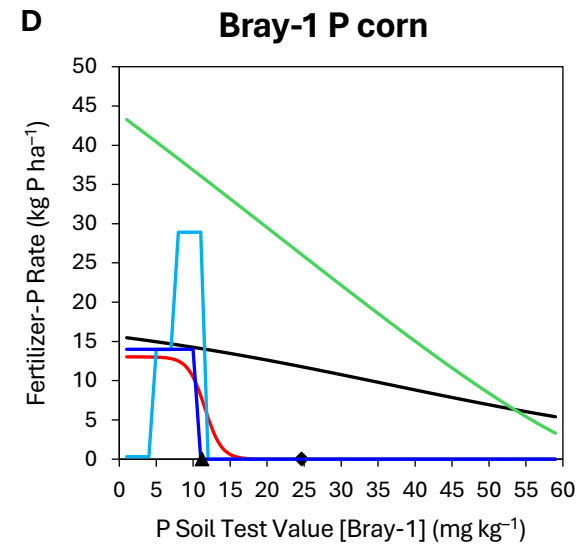
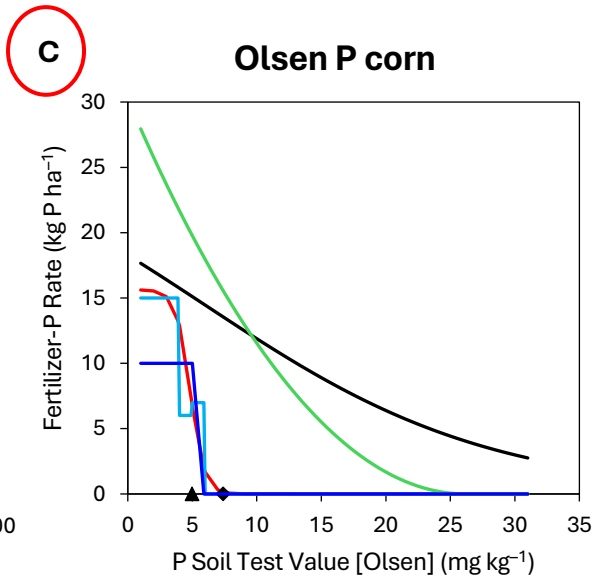
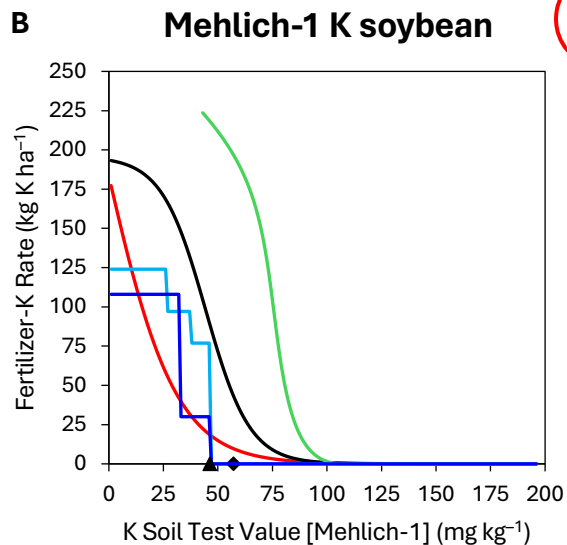
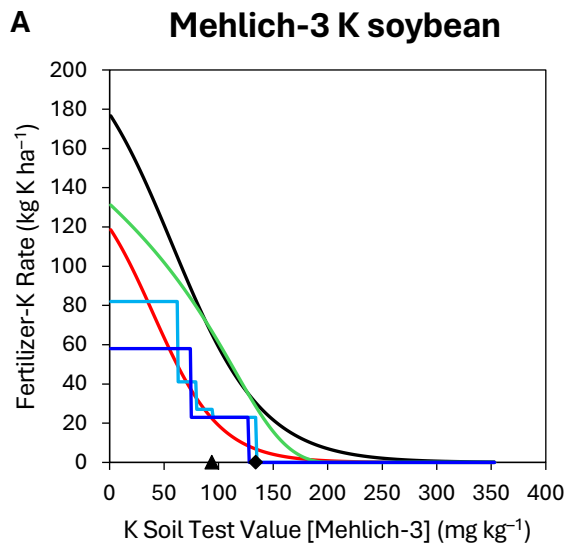
- Limiting applicability in datasets lacking observations at low STVs
- Dual solutions for achieving a target RY
- Training the end-users to interpret the response surface

At agronomically relevant STVs, how different are the recommendations?



- Continuous vs. stepwise behavior
- Overestimation tendencies
- Plateau behavior
- Divergence among frameworks

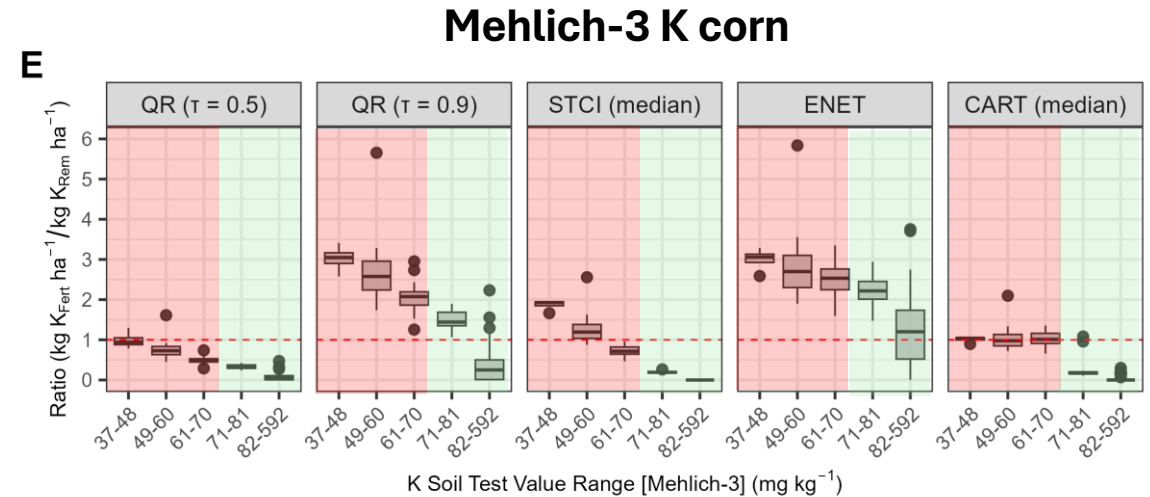
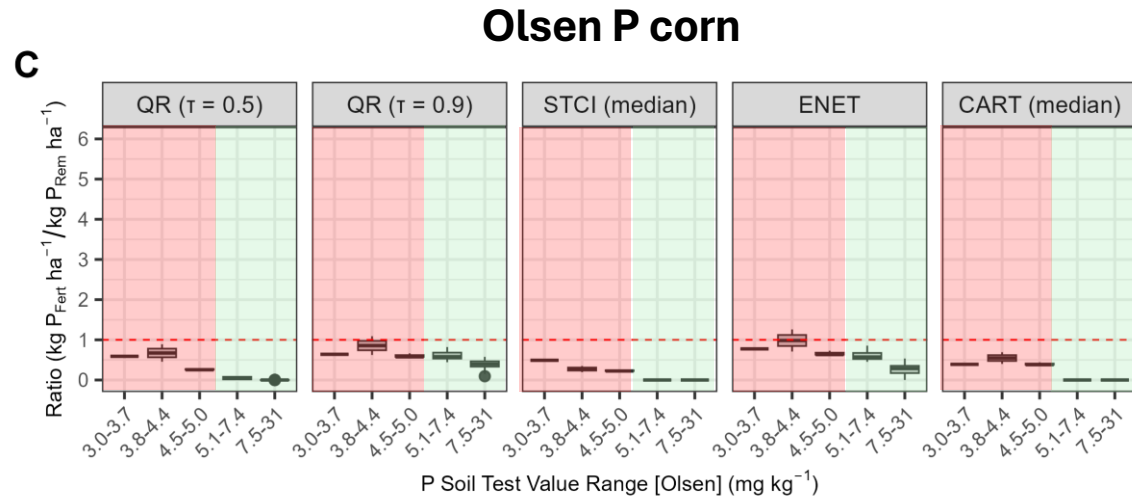
At agronomically relevant STVs, how different are the recommendations?



- Quantile 0.5
- Quantile 0.9
- STCI (median)
- ENET
- CART (median)
- ▲ CSTV
- ◆ Plateau

Dataset	STV mg kg ⁻¹	Quantile (τ = 0.5)	Quantile (τ = 0.9)	STCI (median)	ENET	CART (median)
Estimated fertilizer-P or -K rate (kg ha ⁻¹)						
Olsen P corn	4	13	16	6	22	10
	5	7	15	7	20	10
Mehlich-3 K corn	48	36	118	76	118	41
	70	17	75	29	98	41

Ratio between the estimated fertilizer-nutrient rates and the estimated amount of nutrient removed by grain



- **Ratio = 1.0 (red line):** fertilizer input equals nutrient removal
- **Suboptimal STV (below CSTV):** fertilizer requirements exceed crop nutrient removal
- **Above CSTV:** fertilizer requirements approach or fall below crop nutrient removal

Conclusions

- **Calibration framework selection is a major source of variability in fertilizer recommendations**
- **All frameworks have strengths and limitations that may support or constrain their application for soil test calibration**
- **Quantile regression produced the most consistent and agronomically interpretable recommendations.**
 - Continuous recommendation curve
 - Agronomically realistic fertilizer-nutrient recommendations
 - Flexible recommendations for different risk preferences ($\tau = 0.5$ and $\tau = 0.9$)
 - Potential application for variable-rate nutrient management
- **FRST implementation:**
 - Quantile regression as the primary calibration framework
 - Soil Test Class-Interval (STCI) as a complementary framework

Future efforts to address

- **Economic optimization**
- **Multi-year trial integration**
- **Additional crop response functions**
- **Probability-of-response metrics**

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